

# Design of Cascaded Integrator-Comb Decimation Filters for Direct-RF Sampling Receivers

Takao Kihara, Hiroyuki Yano, Tsutomu Yoshimura

Osaka Institute of Technology, Japan

May 31, 2017

# Outline

## Background and Objectives

## Filter Requirements of CIC Filter

- Output SNR

- Blocker Rejection

## Analysis and Design of CIC Filter

- Folded Quantization Noise

- Folded Out-of-Band Blocker

- Design of CIC Filter

## Simulations

- MATLAB/Simulink Model

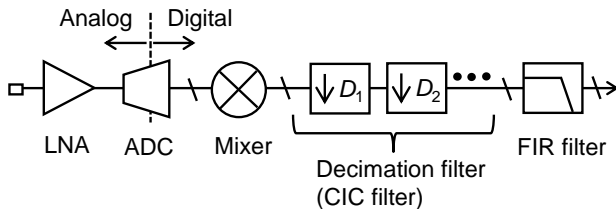
- Input and Output Spectra of CIC Filter

## Summary

# Background

## Direct-RF sampling receivers:

- ▶ Downconvert and filter RF signals in digital domain.
- ▶ Suitable for nano-scale digital CMOS process.
- ▶ Reduce the design cost and time to market.



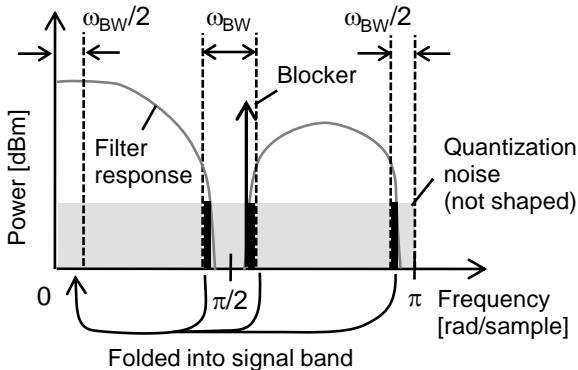
LNA: Low-noise amplifier, ADC: Analog-to-digital converter,  
RFIC '10 [1], A-SSCC '11 [2], JSSC '12 [3]

## Decimation filters:

- ▶ Decrease GS/s rates of an ADC to MS/s rates.
- ▶ Consist of cascaded integrator-comb (CIC) filters.

## Noise and Blockers Folded by Decimation

Quantization noise of the ADC and out-of-band blockers around the notch frequencies are folded into the signal band ( $\omega_{BW}$ ).

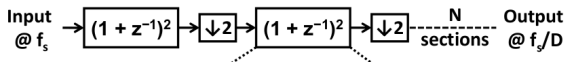


The CIC filter needs to reduce the folded noise and blockers to obtain the required output SNR ( $SNR_{out}$ ).

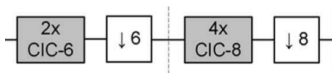
## Objectives

Generally, CIC filters with **some orders** are cascaded (multistage) to achieve the desired sampling rate and required noise level.

- ▶ A-SSCC '11 [2]: Two **2nd-order** CIC filters ( $D = 16$ ,  $D$ : total decimation factor).



- ▶ JSSC '12 [3]: **2nd-** and **4th-order** CIC filters ( $D = 48$ ).



**A higher order:**

- ▶ Provides more attenuation for the folded noise and blockers.
- ▶ Increases the power consumption and area (TCAS-II '01 [4]).

The order should be as small as possible for GS/s CIC filters.

**We present a method to determine the lowest orders of CIC filters.**

## Required $SNR_{out}$ of CIC Filter

- ▶ A RF-direct sampling receiver is assumed to comply with the Bluetooth Low Energy (BLE) specifications.

Block	Performance	Requirement
Receiver	Operating frequency, $f_c$	2400–2483.5 MHz
	Signal bandwidth, $f_{BW}$	~ 1.5 MHz
	Sensitivity	$\leq -74$ dBm
	Output SNR, $SNR_{out}^*$	$\geq 14$ dB
CIC filter	$SNR_{out}^*$	$\geq 14$ dB

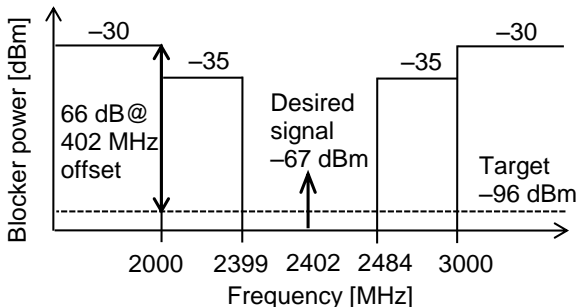
\* Input (desired) power,  $P_{des,RX} = -74$  dBm

- ▶  $SNR_{out}$  is mainly determined from the quantization noise of the ADC.

The CIC filter needs to reduce the folded quantization noise to obtain  $SNR_{out} = 14$  dB for  $P_{des,RX} = -74$  dBm.

## Required Blocker Rejection of CIC Filter

Out-of-band blocking requirements for BLE



- ▶ The CIC filter needs to attenuate the blockers to  $-96$  dBm ( $= -67$  dBm  $- 14$  dB  $- 15$  dB (margin)).

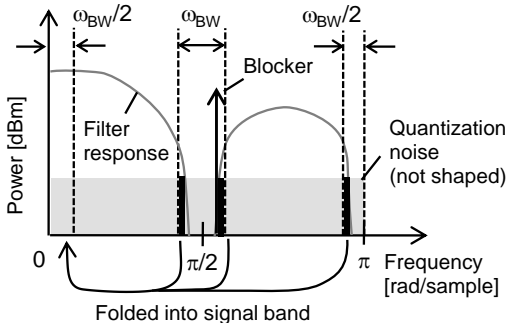
Block	Performance	Requirement
CIC filter	Blocker rejection@ 3–401 MHz offset	61 dB
	≥402 MHz offset	66 dB

## Analysis of Folded Quantization Noise

Quantization noise is folded around the notch frequency,

$$\omega_k = 2k\pi/D \quad (k = \pm 1, \dots, \pm D/2) \text{ for even } D.$$

- ▶  $S_n$ : Power spectrum density of quantization noise
- ▶  $NTF(\omega)$ : Noise transfer function of ADC
- ▶  $H_{CIC}(\omega)$ : Transfer function of CIC filter



Noise power around  $\omega_k$  ( $P_{n,k}$ ) and total noise power folded into  $\omega_{BW}$  ( $P_n$ ):

$$P_{n,k} = \int_{\omega_k - \omega_{BW}/2}^{\omega_k + \omega_{BW}/2} |NTF(\omega)|^2 |H_{CIC}(\omega)|^2 S_n d\omega, \quad P_n = P_{n,0} + 2 \sum_{k=1}^{D/2} P_{n,k}.$$



# Analysis of Folded Out-of-Band Blocker

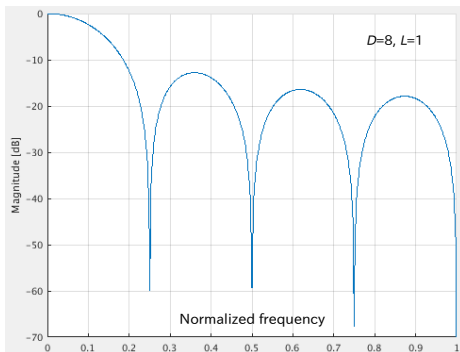
## Worst-case scenario:

Blocker at  $\omega_1 \pm \omega_{BW}$  for  
 $N$ -stage CIC filter

- ▶ Minimum rejection
- ▶ Rejection only from  $N$ th (last) stage,  $|H_{N,CIC}|$

$D_N$ : Decimation factor of  
 $N$ th stage

$L_N$ : Order of  $N$ th stage

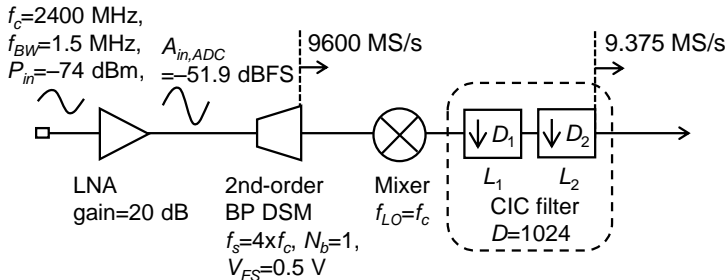


$$|H_{CIC}(\omega_1 \pm \omega_{BW}/2)| \approx |H_{N,CIC}(2\pi/D_N \pm D_1 \cdots D_{N-1}\omega_{BW}/2)|$$

$$= \frac{1}{D_N^{L_N}} \left| \frac{\sin\left(\pi \pm D \frac{\omega_{BW}}{4}\right)}{\sin\left(\frac{\pi}{D_N} \pm \frac{D}{D_N} \frac{\omega_{BW}}{4}\right)} \right|^{L_N} \approx \left(\frac{D\omega_{BW}}{4\pi}\right)^{L_N} = \left(\frac{Df_{BW}}{2f_s}\right)^{L_N}.$$

$D$  and  $L_N$  almost determine the rejection for out-of-band blockers.

## Design of Two-Stage CIC Filter



- ▶ 1-bit 2nd-order band-pass delta-sigma modulator (BP DSM)

Goal: To meet the following requirements with the lowest orders

Block	Performance	Requirement
CIC filter	$SNR_{out}^*$	$\geq 14$ dB
	Blocker rejection <sup>†</sup> @ 3–401 MHz offset	61 dB
	$\geq 402$ MHz offset	66 dB

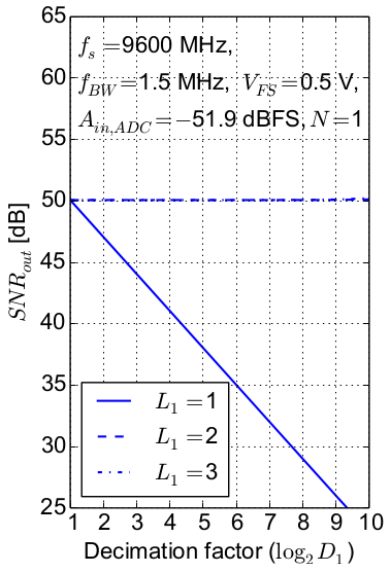
\*  $P_{des,RX} = -74$  dBm, <sup>†</sup>  $P_{des,RX} = -67$  dBm.

## $L_i$ Determined by $SNR_{out}$

Determine a lower limit for  $L_i$  to achieve the required  $SNR_{out}$  for the minimum  $P_{des,RX}$ .

- ▶ One-stage CIC filter with  $L_1$  and  $D_1 = 1024$ .
- ▶ Calculated  $SNR_{out}$  versus  $D_1$  with  $L_1$  as a parameter.
- ▶ For  $L_1 = 1$ ,  $SNR_{out}$  degrades as  $D_1$  increases.
- ▶  $L_1 \geq 2$  keep  $SNR_{out}$  constant for a larger  $D_1$ .

$L_1 = 2$  is selected, because it has little impact on  $SNR_{out}$ .

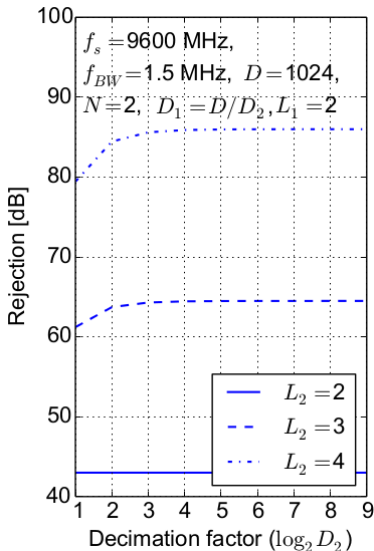


## $L_i$ Determined by Out-of-Band Rejection

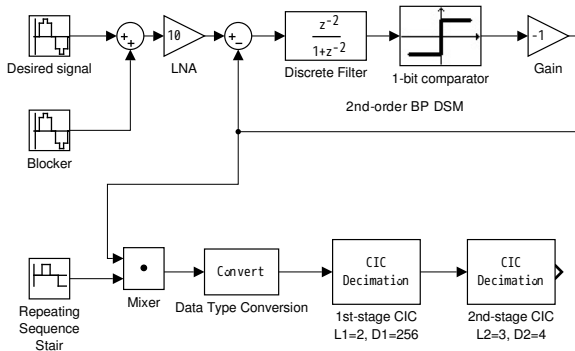
Determine  $L_i$  to achieve the required out-of-band rejection.

- ▶ Two-stage CIC filter with  $L_1 = 2$ ,  $D_1 = D/D_2$ , and  $D = 1024$ .
- ▶ Calculated rejection versus  $D_2$  with  $L_2$  as a parameter.
- ▶ Rejection almost remains constant for  $D_2 \geq 2^2 = 4$ .
- ▶  $L_2 = 3$  and  $D_2 = 4$  provide a rejection of 63 dB, satisfying the requirement.

$L_2 = 3$  and  $D_2 = 4$  are selected, resulting in  $D_1 = 256$ .

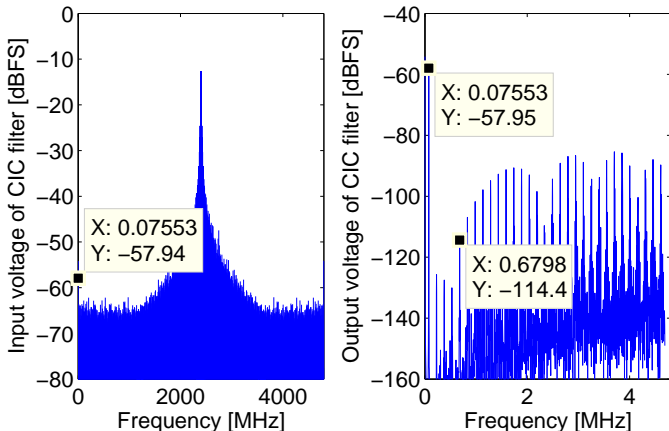


# MATLAB/Simulink Model



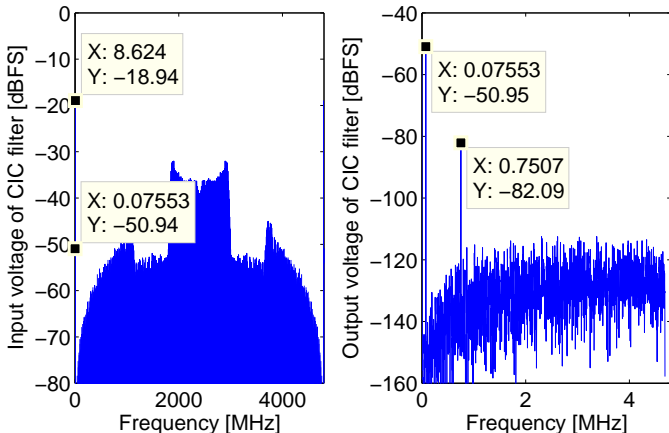
- ▶ Direct-RF sampling receiver designed on MATLAB/Simulink.
- ▶ CIC filters: 2nd-order stage with  $D_1 = 256$  and 3rd-order one with  $D_2 = 4$  ( $D = 1024$ ).
- ▶ Desired frequency:  $f_c + f_{BW}/(2 \cdot 10) = 2400.075$  MHz.

# Simulated Spectra for Minimum Desired Power



- ▶  $P_{des,RX} = -74$  dBm without a blocker.
- ▶ Achieved  $SNR_{out}$  of 53.5 dB (=  $-57.9$  dBFS + 114.4 dBFS).

## Simulated Spectra with Blocker



- ▶  $P_{des,RX} = -67$  dBm with  $-35$ -dBm blocker at 8.625-MHz offset (worst case).
- ▶ Achieved rejection of 63.1 dB ( $= -18.94$  dBFS + 82.1 dBFS).

## Summary

- ▶ Derived analytical expressions for  $SNR_{out}$  and out-of-band rejection of a multi-stage CIC filter.
- ▶ Presented a method to determine the lowest order of each CIC filter.
  - ▶ Enable a RF-direct sampling receiver to satisfy the  $SNR_{out}$  and out-of-band blocking requirements of BLE.
- ▶ Calculations agree well with simulations.

Performance	Required	Simulated	Calculated
$SNR_{out}^*$	> 14 dB	53.5 dB	50.0 dB
Blocker rejection <sup>†</sup> @			
8.625 MHz offset	61 dB	63.1 dB	63.7 dB
411.75 MHz offset	66 dB	110.4 dB	110.1 dB

\* $P_{des,RX} = -74$  dBm,

The presented method can reduce the power consumption and chip area of GS/s CIC filters.